



Reliability in Observational Research: Assessing Covariate Imbalance in Small Studies

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Large-scale propensity score (LSPS)

- A **systematic** approach to propensity adjustment
- Use a large set of covariates ($10,000 < n < 100,000$)
- But don't want to balance *everything*
 - Mediators – pre-treatment
 - Simple colliders – pre-treatment
 - Instruments – diagnostics, domain knowledge
 - M-bias – correlation with underlying causes
- Fit a propensity model
 - LASSO (regularized regression) because $\#variables > \#cases$
- Match or stratify on propensity score
- Diagnostic: check that covariate balance is achieved on all observed variables



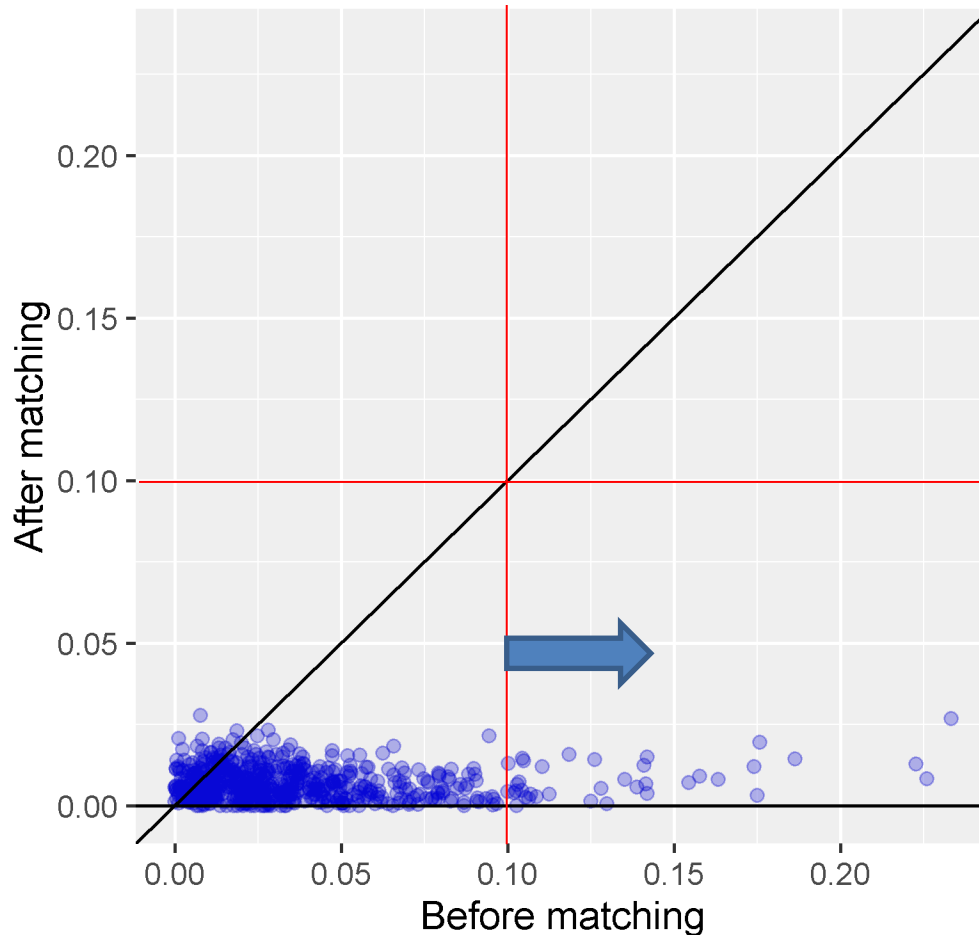
How do you know you succeeded?

- Whether you balance 5 or 50,000 covariates that are potential confounders, how do you know it worked?



Diagnostic: Covariate balance

Standardized difference of mean



Plot 60,000 covariates;
most are binary:

$$\frac{\text{abs}(P_{\text{target group}} - P_{\text{comparator group}})}{\text{standard deviation}}$$

Normand 2001, Austin 2007:
Standardized mean difference
< 0.1



Problem for today

- As sample size falls, you always fail your diagnostics with chance imbalance
 - What to do different?



Covariate balance review

- Covariate balance is an important diagnostic for PS adjustment in cohort studies (1/3rd) [Granger 2020]
- The goal is not to detect imbalance, but to detect substantial imbalance [Austin 2009, ...]
 - Else as sample size rises and therefore precision of SMD rises, all studies will be rejected
- The most common solution is to check for $|SMD|$ over 0.1 (or 0.25) [Austin 2009, ...]



Reject small cohorts for chance imbalance

- Imbalance by chance

$$P(\text{false rejection}) = 1 - \left(2\Phi\left(\frac{\sqrt{N}}{20}\right) - 1 \right)^J$$

- Total sample of 250 and 5 covariates, 90% chance of rejecting study as imbalanced (SMD>0.1)
- Total sample of 1000 and 20 covariates, 90%
- As covariates increase, more chance rejection



Idea

- Check not for nominally exceeding a threshold, but for statistically significantly exceeding the threshold
 - As sample size falls, the threshold allows more imbalance but the corresponding wider effect CI tolerates more bias
 - Confounding could shift effect estimate 1.2 to 1.4 but CI is 0.7 to 3
 - The CI is designed to accommodate chance imbalance, so no reason to reject studies with chance imbalance
- Try this new rule in simulation and RWD



Standardized mean difference (SMD)

- $sd_j = \sqrt{\frac{\left(\frac{s_{1,j}}{n_1}\right)\left(\frac{1-s_{1,j}}{n_1}\right) + \left(\frac{s_{0,j}}{n_0}\right)\left(\frac{1-s_{0,j}}{n_0}\right)}{2}}$
- $smd_j = \frac{\frac{s_{1,j}}{n_1} - \frac{s_{0,j}}{n_0}}{sd_j}$
- $varsmd_j = \frac{n_1+n_0}{n_1n_0} + \frac{smd_j^2}{2(n_1+n_0-2)}$



Three primary rules

- **All** – accept all studies (ignore imbalance)
 - Imbalance commonly ignored
- **Nominal** – reject studies with any covariate $|SMD|$ is greater than 0.1
 - Most common threshold when one is used
- **Signif** – reject studies with any covariate $|SMD|$ statistically significantly greater than 0.1 after Bonferroni correction for #covariates
 - Our proposal



Three rules, two levels

- Rules
 - **All** – accept all studies (ignore imbalance)
 - **Nominal** – reject studies any $|SMD| > 0.1$
 - **Signif** – reject studies any $|SMD|$ statistically significantly > 0.1 after Bonferroni
- Levels
 - Database
 - Apply rule to each covariate, reject some databases
 - Network
 - Random effects model (R rma) on the SMDs for each covariate across non-rejected databases
 - Apply the rule to the meta-analytic estimates, potentially reject whole network study

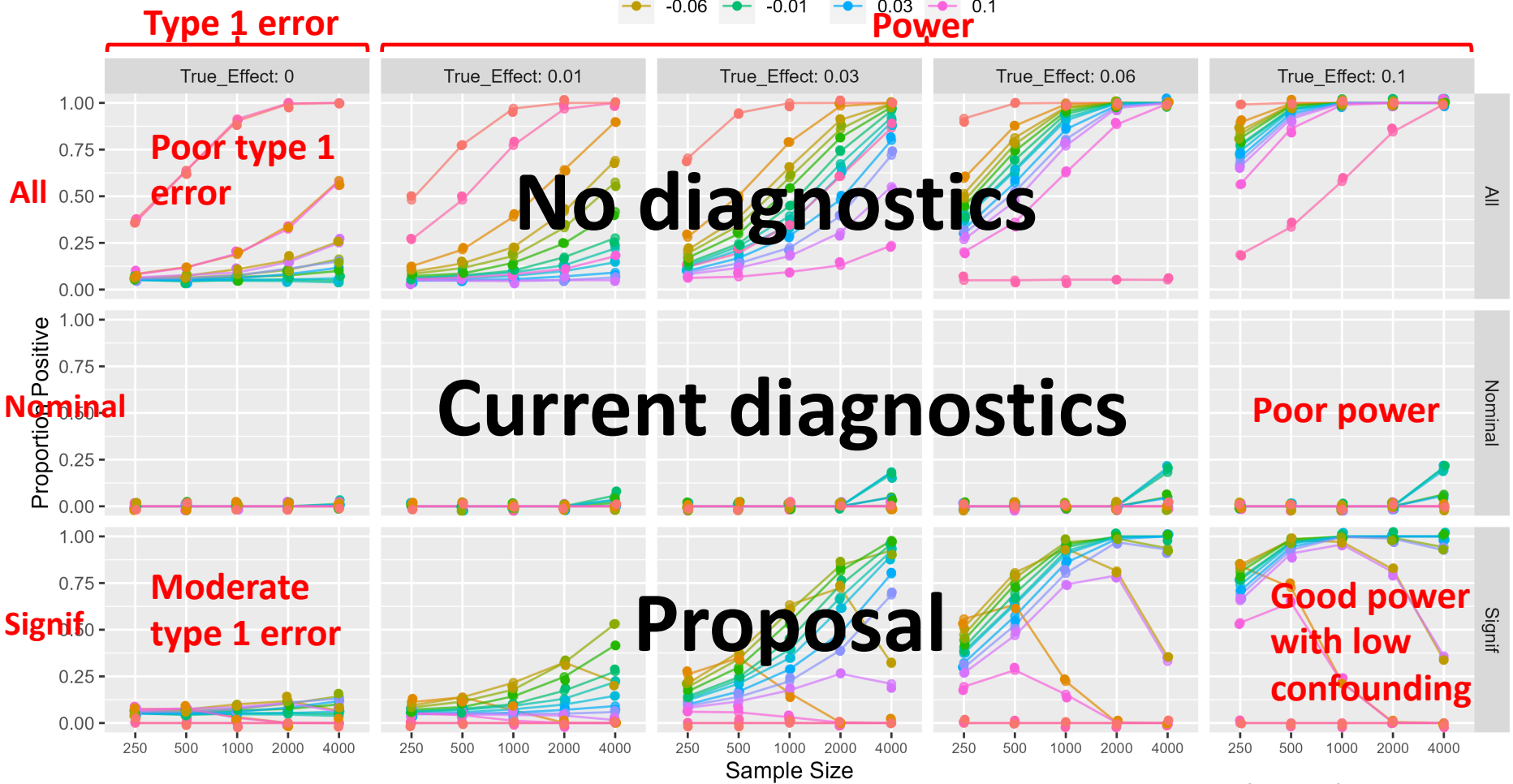
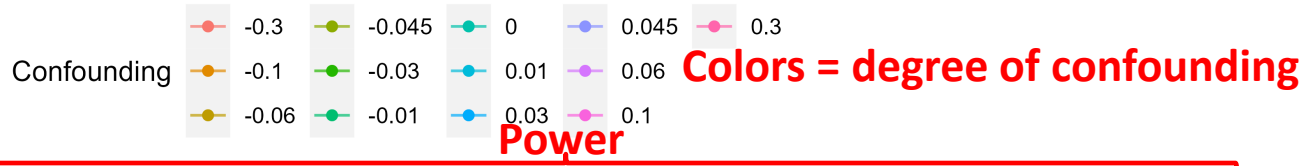


Metrics

- Type 1 error rate
 - Among studies with no true effect
 - Numerator – # not rejected and effect $p < 0.05$
 - Denominator – total number of studies
- Power
 - Among studies with a true effect
 - Numerator – # not rejected and effect $p < 0.05$
 - Denominator – total number of studies



Rule performance at the database level on simulation

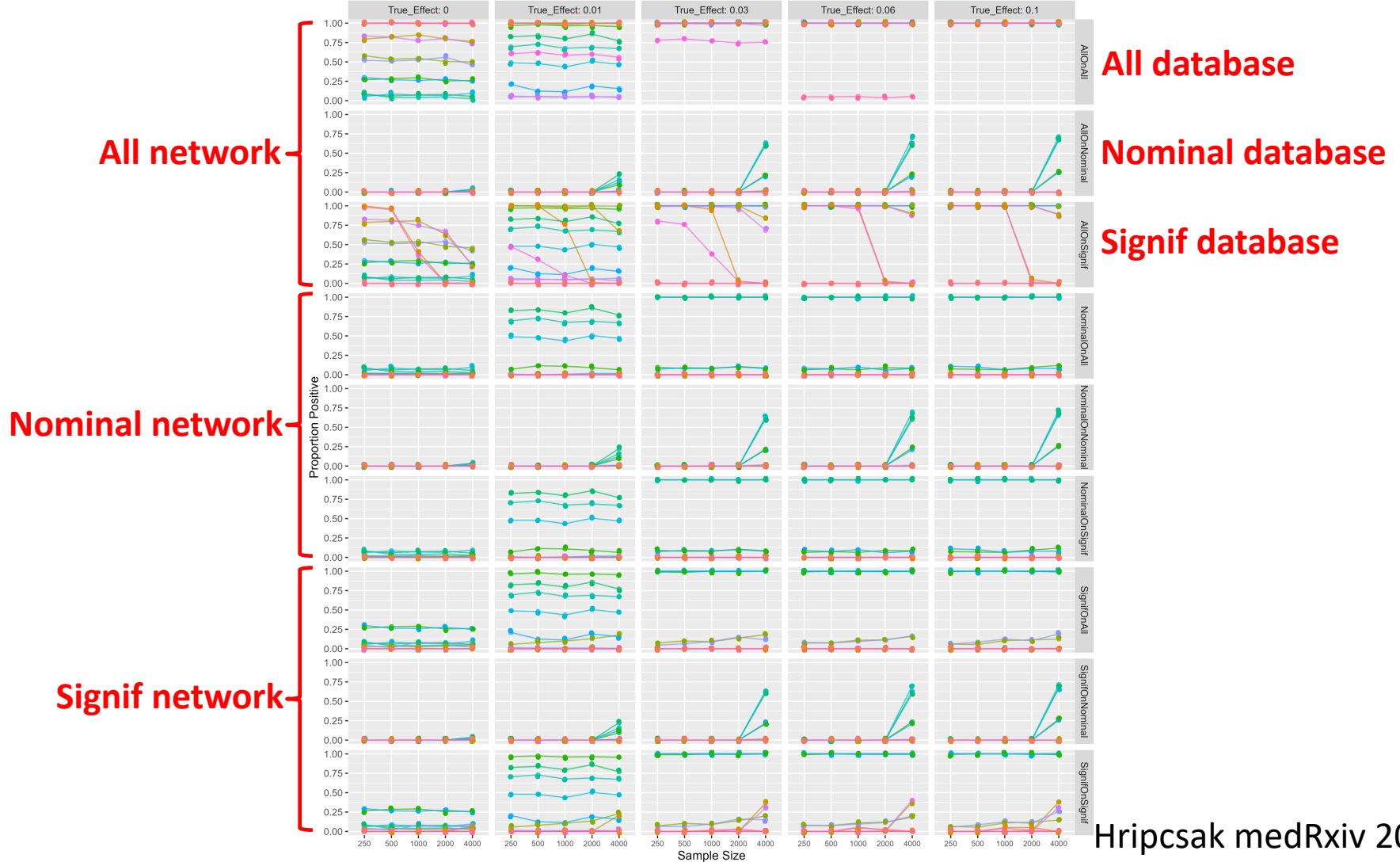
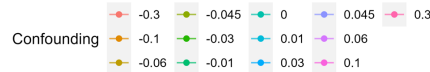


Sample size (250-4000)

Hripcsak medRxiv 2024



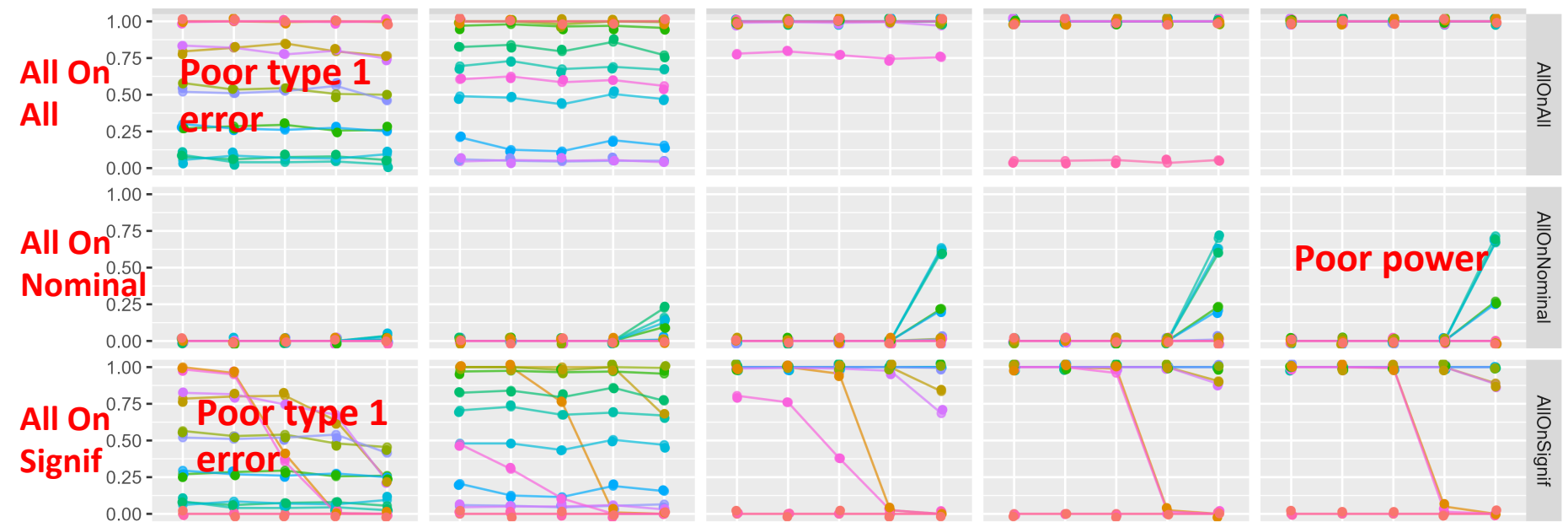
Rule performance at the network level on simulation





Rule performance at the network level on simulation

- All network = no network diagnostic
 - Three rows fail
 - Note: Signif just at database level fails
 - Network improves precision of effect estimate but not of SMD

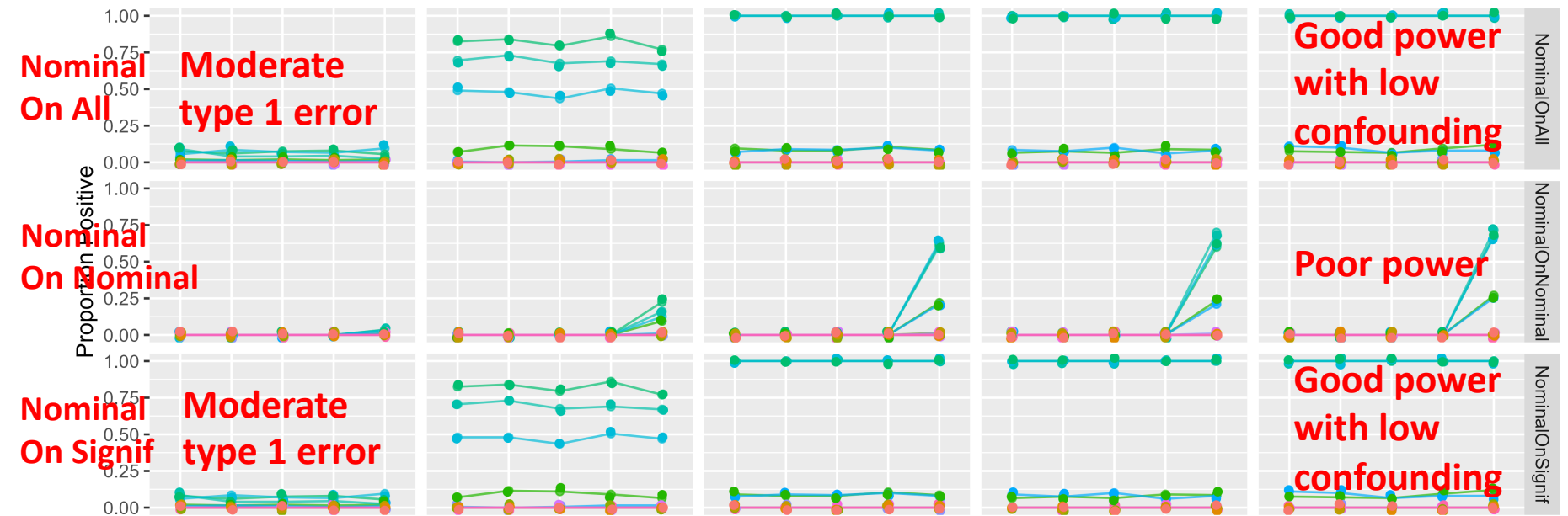


Cannot ignore balance at the network level



Rule performance at the network level on simulation

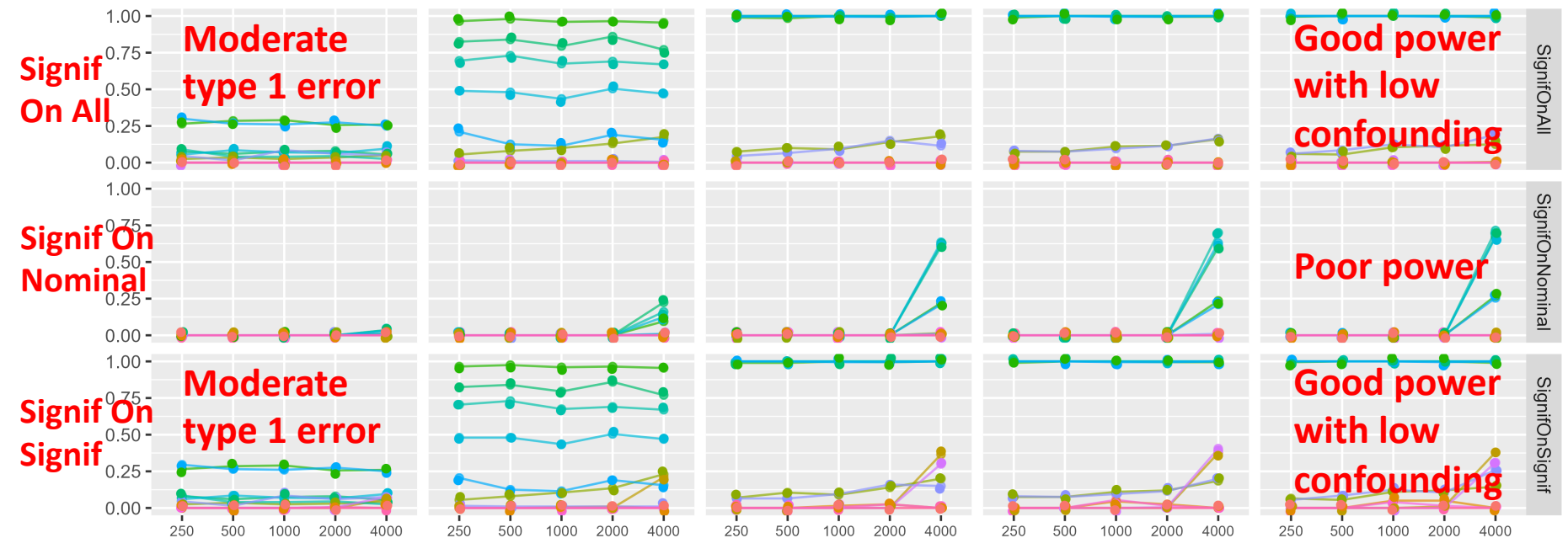
- Nominal at network level
 - Nominal-On-All, Nominal-On-Signif good here
 - Meta-analysis has enough power to avoid failing by chance





Rule performance at the network level on simulation

- Signif at network level
 - Signif-On-All, Signif-On-Signif good here
 - But higher type 1 error





Rule performance at the network level on simulation

- These seem to work with moderate excess type 1 error but good power
 - Nominal-On-All
 - Nominal-On-Signif
 - Signif-On-All
 - Signif-On-Signif

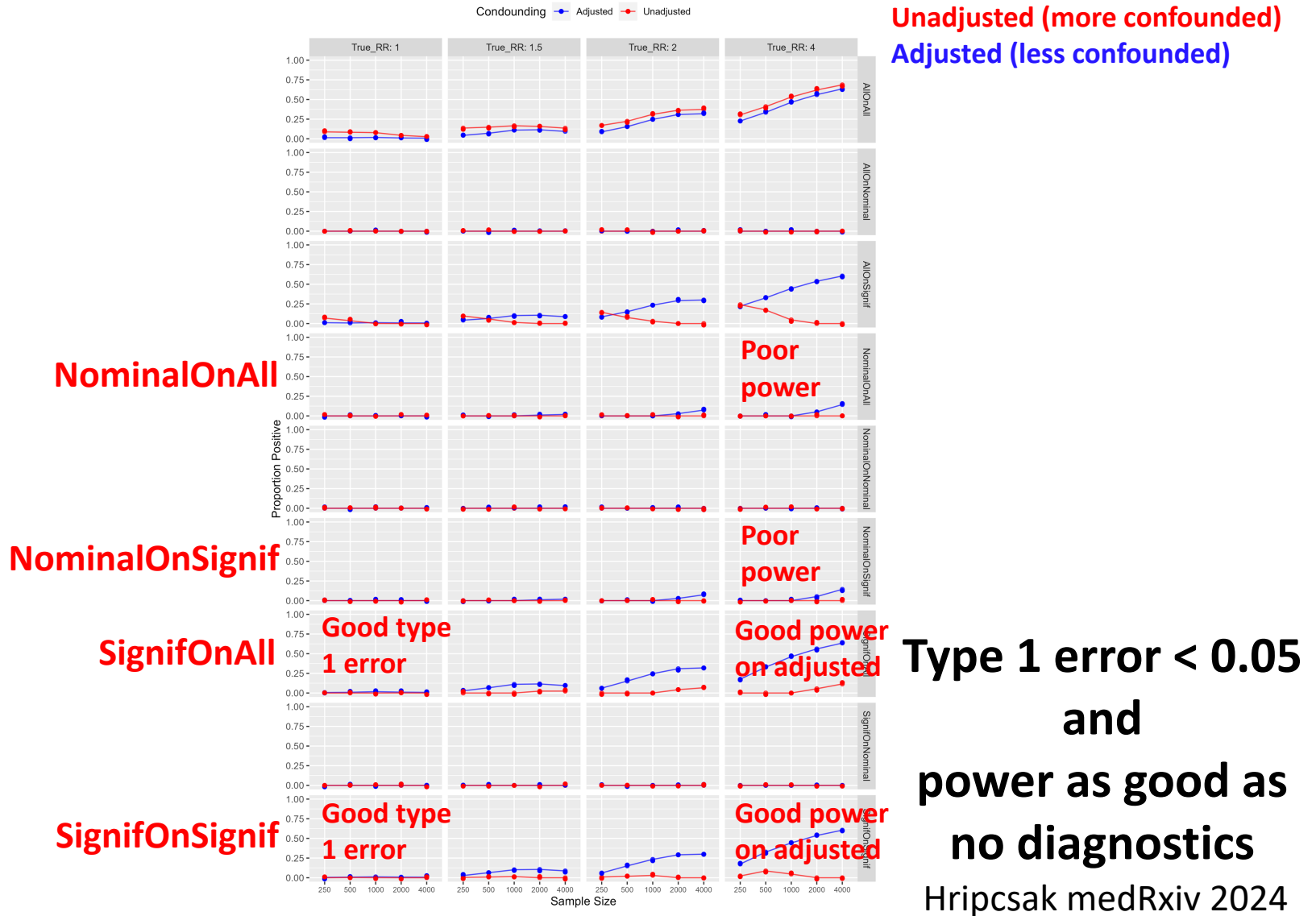


Real-world data

- Reused data from OHDSI LEGEND hypertension and type 1 diabetes studies
 - [Suchard Lancet 2019, Khera BMJ Open 2022]
 - Four treatment comparisons
 - lisinopril vs hydrochlorothiazide, lisinopril vs metoprolol, sitagliptin vs liraglutide, sitagliptin vs glimepiride
 - 110 real negative controls (hazard ratio 1)
 - Corresponding synthetic positive controls (HR 1.5, 2, 4)
 - L1-regularized Poisson regression model
- Data and analysis
 - Three sources: Merative Medicare, Merative Medicaid, Optum EHR
 - 20,000 cases divided among “databases” with 250 to 4000 cases
 - 98,681 covariates, built a large-scale propensity model
 - Several analytic methods: unadjusted (crude) versus adjusted
 - Cox proportionate hazards model on matched or stratified sample or crude sample



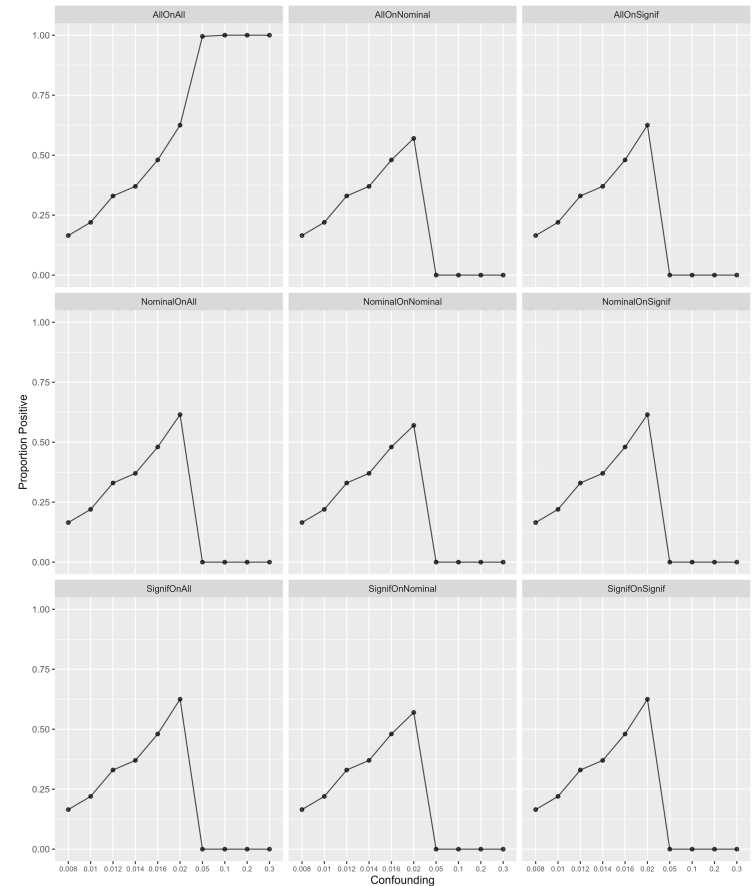
Rule performance at the network level on real-world data





Shouldn't type 1 error be 0.05?

- Given a threshold on SMD, it is possible to create a bad-case simulation scenario
 - Typical study with 20,000 cases and 20 covariates under no true effect but with confounding, all 9 rules get type 1 error over 0.5
- We purposely found the weak points using our simulation
 - Could do Bayesian analysis
 - Probability of getting these parameters under reasonable priors is low (thus RWD result)

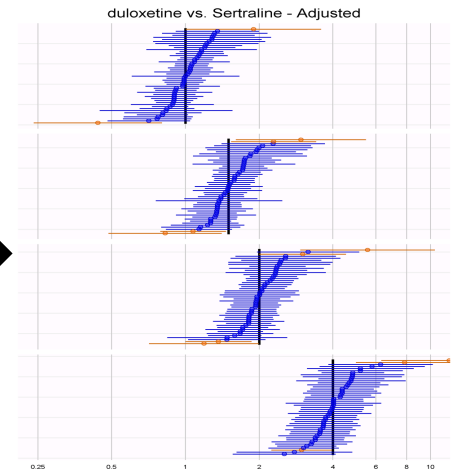
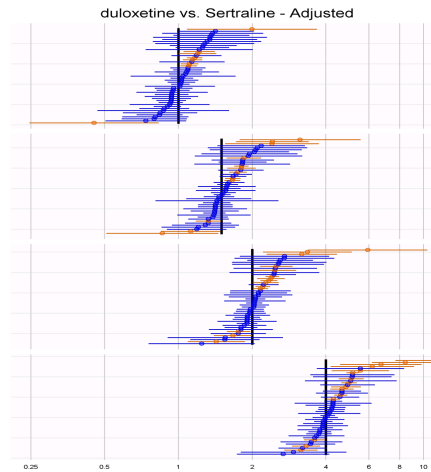
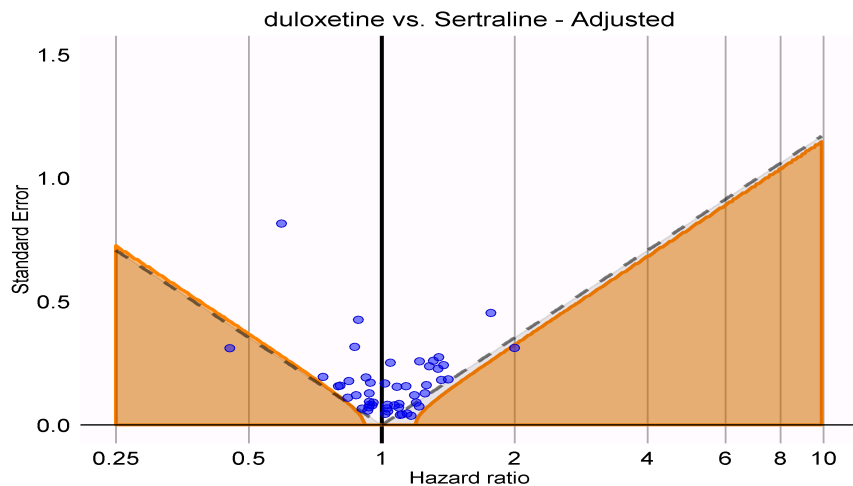




Can correct for type 1 error

Confidence interval calibration using **negative controls**: residual bias

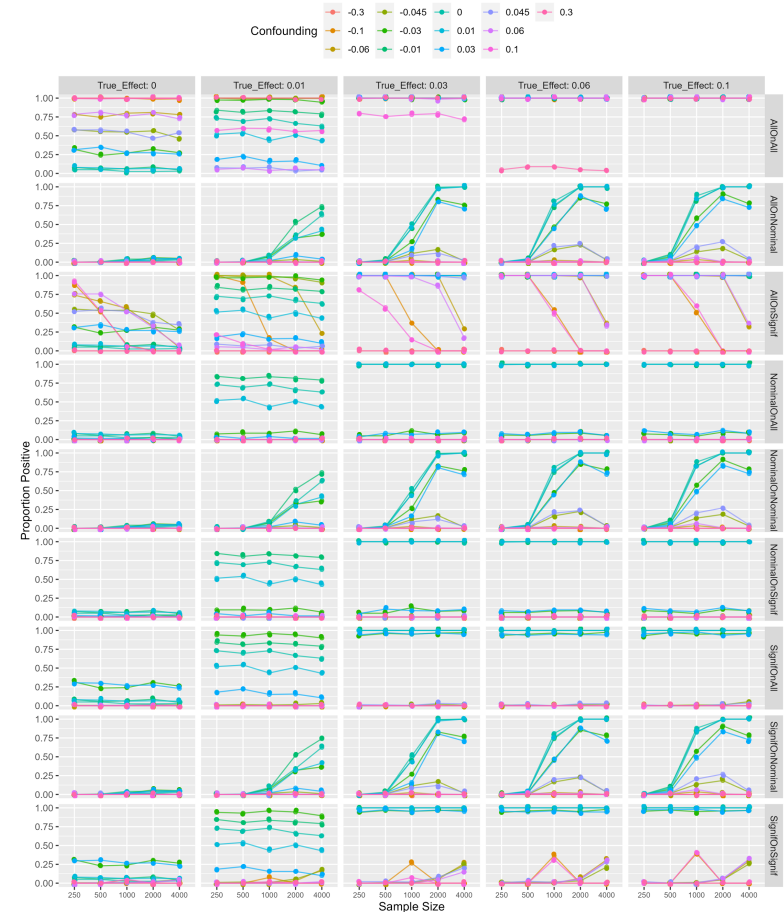
- Address residual confounding using hypotheses you know the answer for
 - 50 to 100 controls
- If too many are positive, then systematic error is operative
- Calibrate to keep the type 1 error at 0.05





Same results for 20 covariates

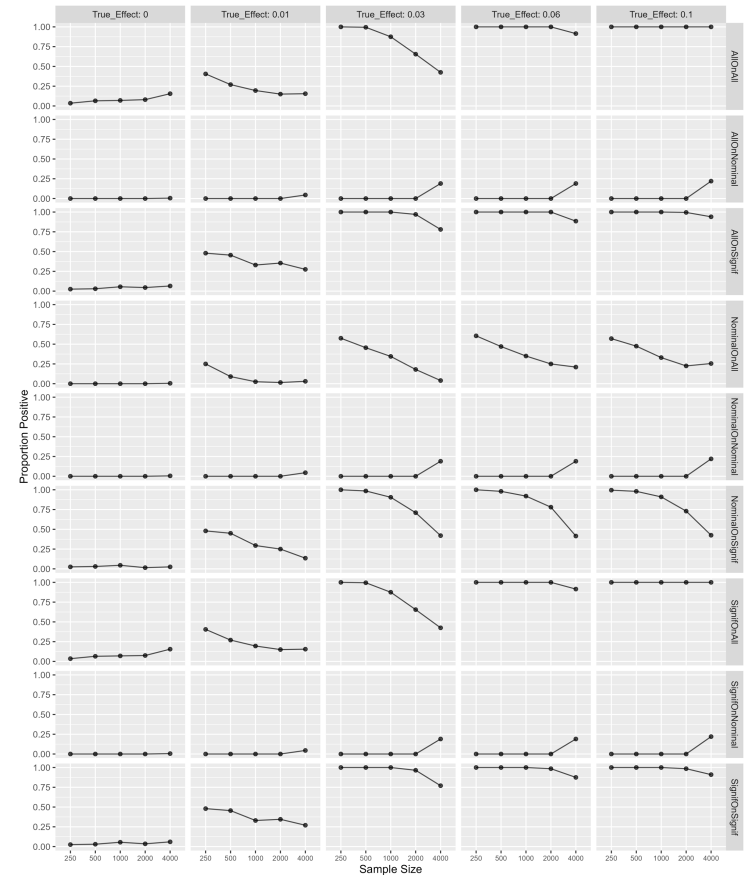
- Curve shifted to the left, but same pattern and tradeoff for type 1 error versus power





What if confounding is heterogeneous?

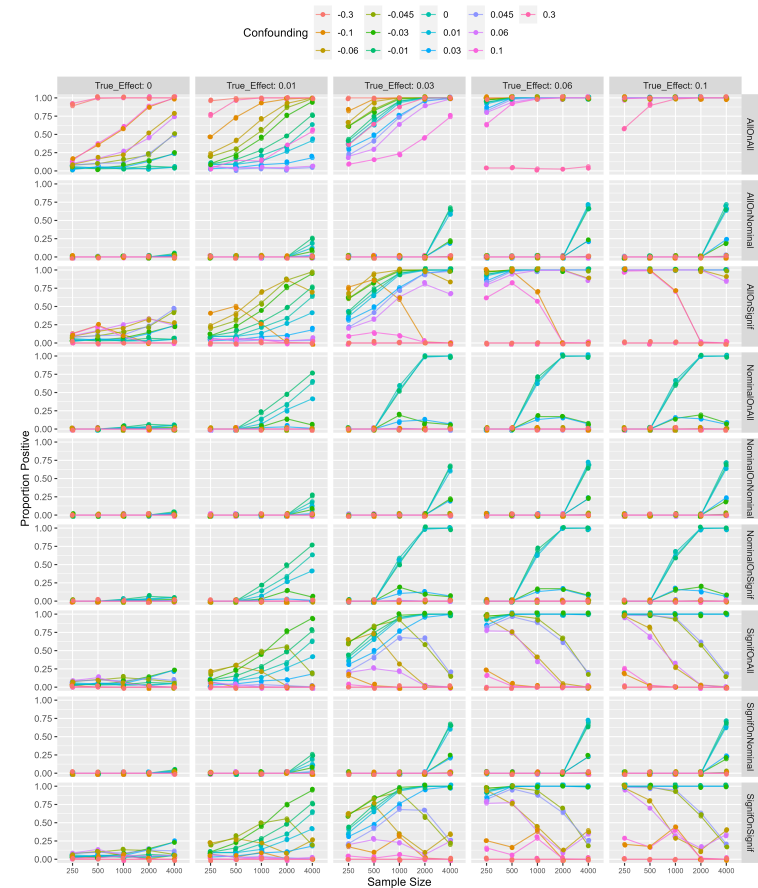
- The effective rules still work
 - Signif-On-Signif has a little more power and a little less type 1 error than Signif-On-All





What if only 5 databases

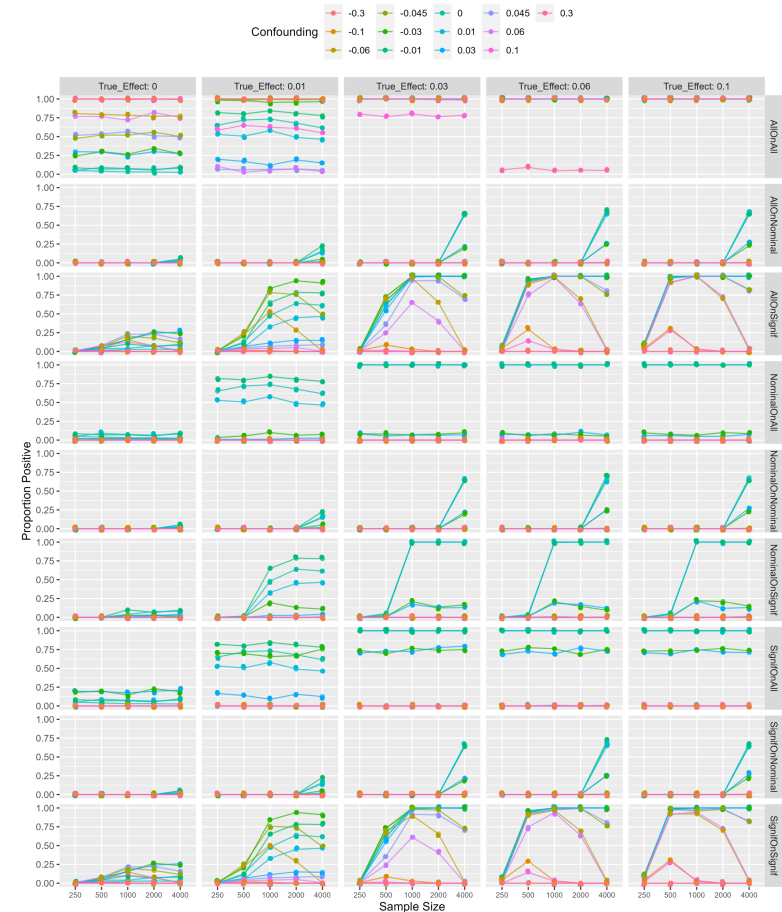
- Nominal at network level (which appeared otherwise to have potential in simulations) loses all power on smaller databases
 - Meta-analysis of the SMDs no longer gain enough precision to avoid chance rejection
- Thus even simulation favors Signif-On-Signif





Is Bonferroni correction needed?

- Eliminating the Bonferroni correction does not improve the type 1 error rate but does drop power to 0 at the smallest sample sizes





Doesn't increasing # covariates hide confounding?

- Bonferroni correction for many covariates effectively raises the SMD threshold; doesn't that unfairly allow more confounding?
- If we have actual knowledge that there is no confounding, then follow that
 - (never happens)
- Otherwise, assume confounders distributed in the covariates
 - Probability 0.001 of covariate being imbalanced
 - Sample size 4000; 10,000 covariates; reject 0.62 of studies
 - With 60,000 covariates, rose to 1.0
- Bonferroni does **not** overwhelm imbalance detection



Can you produce a good PS model in such small databases?

- Yes
 - Using same data sources and hypotheses
 - Worked well ≥ 1000 , usually > 250 , sometimes 125
 - [Schuemie OHDSI 2023]



Conclusions

- **Small cohorts result in rejection for chance imbalance ($SMD > 0.1$) and zero power**
- As sample size falls, effect CIs lengthen, rendering small confounding less important
 - Using a statistical test for sufficient imbalance raises the threshold where a given degree of confounding is tolerable
- Our results comparing no diagnostic (old), nominal threshold (old), statistical test (new)
 - **Statistical test maintains the best type-1-error to power balance across the simulations and RWD**



Conclusions

- Meta-analysis of network studies may produce a more precise effect estimate
 - Therefore you also need a more precise diagnostic for imbalance, else systematic bias will predominate
 - Our results show that meta-analysis of SMDs and a statistical test produce the best type-1-error to power balance

Must do meta-analysis of diagnostics



Conclusions

- The statistical test for imbalance makes it feasible to check thousands of covariates
 - Regardless of how many confounders are adjusted for, the data set includes information about imbalance and the effect of potential confounding
 - **Not checking for imbalance on all covariates is a head-in-the-sand approach**
 - Imbalanced variables should be justified as known or proven instruments



Recommendations

- For PS-adjusted cohort studies, check for imbalance of covariates
- **Check for imbalance (SMD) statistically significantly greater than 0.1 (or other pre-specified threshold) in any covariate after Bonferroni correction**
- **Network studies require meta-analysis of each covariate and checking for statistically significant imbalance (at database and network level)**
- **Check all available covariates, not just the ones adjusted for**



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